

CAREERS360

GOA BOARD SSC

MATHS

Question Paper



2018 IV 04

0930

Seat No. :

| | | | | |
|--|--|--|--|--|
| | | | | |
|--|--|--|--|--|

Time : 2½ Hours

MATHEMATICS (E)

Subject Code

| | | | |
|---|---|---|---|
| S | 0 | 2 | 1 |
|---|---|---|---|

Total No. of Questions : 8

(Printed Pages : 8)

Maximum Marks : 80

- INSTRUCTIONS:**
- i) Answer each main question on a **fresh** page.
 - ii) All questions are **compulsory**.
 - iii) The question paper consists of 8 questions, **each of 10 marks**.
 - iv) There is no overall choice. However, internal choice has been provided in 3 questions of 3 marks **each**.
 - v) In questions on constructions, the drawing should be clear and exactly as per the given measurements. The construction lines and arcs should also be **maintained**.
 - vi) Graph paper will be supplied on request.
 - vii) Use of calculator and Mathematical tables is not permitted.

1. A) Select and write the most appropriate alternative from those given below : [1]
If α and β are the zeroes of the polynomial $x^2 + 6x + 5$ then $(\alpha + \beta)^2 =$ _____
a) -36 b) -6 c) 6 d) 36
B) Using Euclid's division algorithm find the H.C.F. of 255 and 867. [2]
C) Assuming that $\sqrt{5}$ is an irrational number, prove that $2 + 3\sqrt{5}$ is also an irrational number. [3]
D) If $\sqrt{3}$ and $-\sqrt{3}$ are the zeroes of the polynomial $2x^4 - 3x^3 - 5x^2 + 9x - 3$. Find the other two zeroes of the polynomial. [4]
2. A) Select and write the most appropriate alternative from those given below : [1]
One card is drawn from a well shuffled deck of 52 cards. The probability of getting a face card is _____
a) $\frac{1}{52}$ b) $\frac{3}{52}$ c) $\frac{3}{13}$ d) $\frac{1}{4}$



- B) A die is thrown once. Find the probability that the number appears on the top face of the die is [2]
- i) a prime number
 - ii) more than 4.
- C) Find the roots of **any one** of the following quadratic equations : [3]
- i) $8x^2 - 14x + 5 = 0$ (By factorisation method)
 - ii) $2x^2 - 7x + 3 = 0$ (By completing the square method).
- D) Find two consecutive odd positive integers, sum of whose squares is 394. [4]
3. A) Select and write the most appropriate alternative from those given below : [1]
If $7x + 3y = 11$ and $3x + 7y = -1$ then $x - y =$
a) 3 b) 4 c) 10 d) 12
- B) The following is a pair of linear equations in two variables :
 $7x - 5y = 4$ and
 $14x + ky = -4$.
Answer the following questions with reference to the given pair of equations : [2]
- i) Write down the condition for unique solutions.
 - ii) Find the value of k.
- C) Find the solution of **any one** of the following pair of linear equations : [3]
- i) $2x + 3y = 5$ and
 $3x + 4y = 6$ (By elimination method)
 - ii) $x - 4y = 11$ and
 $2x + 5y = -4$ (By cross-multiplication method)
- D) Find the solution of the following pair of linear equations graphically : [4]
 $2x + y = 7$ and
 $x + 2y = 8$
Rewrite and complete the following tables.
 $2x + y = 7$ $x + 2y = 8$
- | | | | |
|----------|--|--|--|
| x | | | |
| y | | | |
- | | | | |
|----------|--|--|--|
| x | | | |
| y | | | |
- (Plot atleast 3 points for each line using a graph paper)



4. A) Select and write the most appropriate alternative from those given below : [1]
 The 12th term of the arithmetic progression 9, 14, 19, 24 is _____
 a) 45 b) 46 c) 54 d) 64
- B) The following table shows the daily income of 50 workers : [2]

| Daily Income (in Rs.) | Number of Workers |
|--------------------------|-------------------|
| 100 – 400 | 18 |
| 400 – 700 | 15 |
| 700 – 1000 | 10 |
| 1000 – 1300 | 7 |

Find the Median of the above given data.

- C) A man bought a scooter with 12 monthly instalments. He paid ₹ 6,000 as first instalment and thereafter for each instalment he paid ₹ 250 less than the previous month. By instalment if he paid ₹ 3,150 extra over the original price, then find the original price of the scooter. [3]
- D) The following table shows the marks scored by 40 students in Mathematics :

| Marks Scored (C.I.) | No. of Students (f _i) | Class Mark (x _i) | Deviation d _i = x _i – a | f _i d _i |
|------------------------|--------------------------------------|---------------------------------|--|---|
| 0 – 10 | 2 | – | – | – |
| 10 – 20 | 5 | – | – | – |
| 20 – 30 | 14 | – | – | – |
| 30 – 40 | 9 | – | – | – |
| 40 – 50 | 6 | – | – | – |
| 50 – 60 | 4 | – | – | – |
| Total | $\sum f_i = 40$ | | | $\sum f_i d_i = \underline{\hspace{2cm}}$ |

Taking the class mark denoted by 'a' of the class-interval 20 – 30 as the assumed mean, rewrite and complete the table and also find the mean of the marks by the assumed mean method. [4]

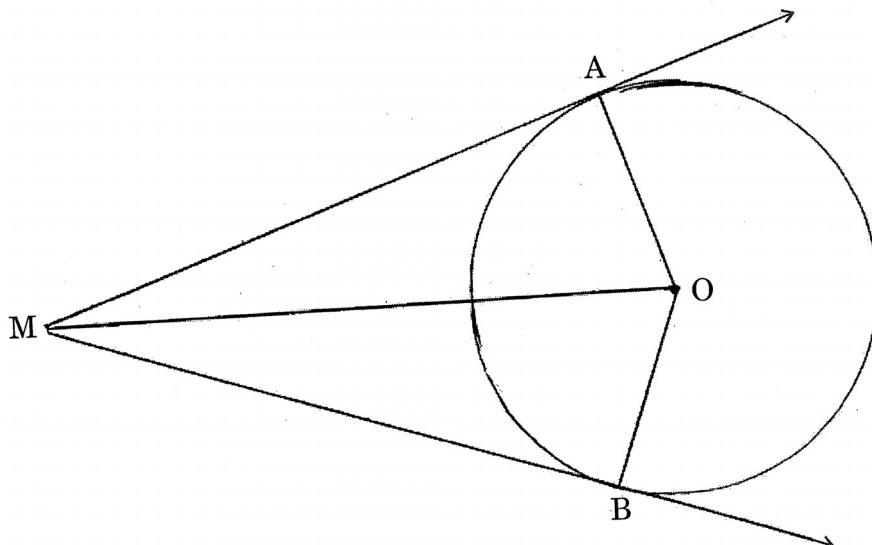


5. A) Select and write the most appropriate alternative from those given below : [1]

RP and RQ are tangent segments drawn from an external point R to a circle with centre O. If $\angle QRO = 35^\circ$ then the measure of $\angle POQ = \underline{\hspace{2cm}}$

- a) 55° b) 70° c) 110° d) 145°

B) Given : Point O is the centre of a circle. MA and MB are two tangent segments drawn from an external point M to the circle at A and B respectively. Prove that : $MA = MB$. [3]



(Write only the proof with reasons)

C) Draw a circle with centre O and radius 2.7 cm. Take a point P at a distance 8.5 cm from the centre of the circle. Using a pair of compasses and ruler, construct two tangents PS and PT to the circle. Measure and state the length of the tangent segments. [3]

D) Using a pair of compasses and ruler, construct $\triangle ABC$ with sides $AB = 8\text{ cm}$, $BC = 9.5\text{ cm}$ and $AC = 6.5\text{ cm}$. Then construct $\triangle A'BC'$ whose sides are $\frac{3}{4}$ of the corresponding sides of $\triangle ABC$. [3]

6. A) Select and write the most appropriate alternative from those given below : [1]

If $\triangle ABC$ is right angled at C, then the value of $\sin(A + B) = \underline{\hspace{2cm}}$

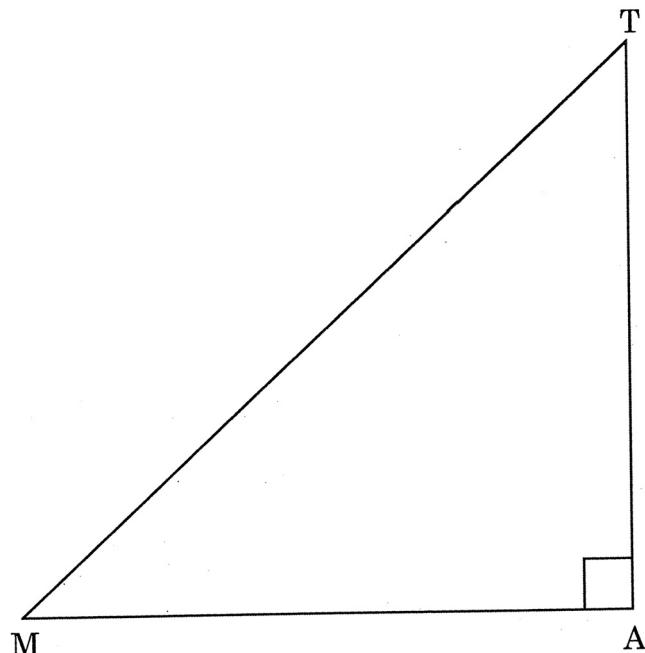
- a) 0 b) 1 c) $\frac{1}{2}$ d) $\frac{\sqrt{3}}{2}$



B) Attempt **any one** of the following :

[3]

- i) In $\triangle MAT$, $\angle A = 90^\circ$ and $\tan M = \frac{24}{7}$, then find :



- a) The length of MT
 - b) The value of $\cos M$
 - c) The value of $\sec T$.
- ii) Evaluate the following expression using known numerical values of trigonometric ratios :
$$5 \sin^2 30^\circ - 4 \cos^2 30^\circ + 6 \cot^2 60^\circ.$$

C) Prove the following identity :

[2]

$$\sqrt{\frac{1-\cos A}{1+\cos A}} = \operatorname{cosec} A - \cot A$$

D) Attempt the following :

- i) Find the coordinate of the point which divides the line segment joining the points $(2, -1)$ and $(-3, 4)$ internally in the ratio $3 : 2$. [2]
- ii) Find the area of $\triangle PQR$ whose vertices are $P(5, 2)$, $Q(-3, 7)$ and $R(2, -4)$. [2]

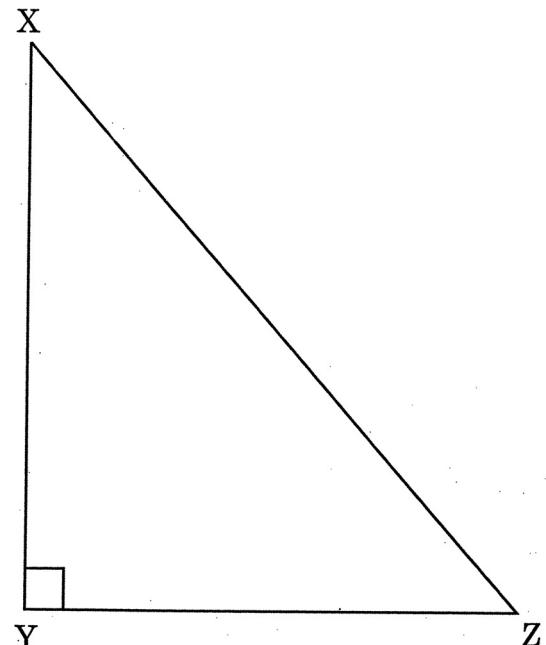
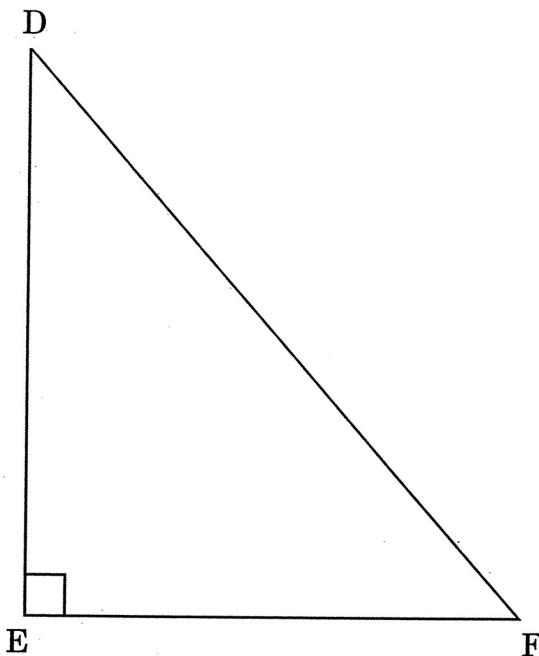


7. A) Select and write the most appropriate alternative from those given below : [1]

$\triangle ABC \sim \triangle PQR$ and $\text{ar}(\triangle ABC) = 144 \text{ cm}^2$, $\text{ar}(\triangle PQR) = 81 \text{ cm}^2$. If $QR = 27 \text{ cm}$
then $BC = \underline{\hspace{2cm}}$ cm.

- a) 9 b) 12 c) 36 d) 48

B) With reference to the given figure and the given conditions write only the proof with reason of the following theorem. [3]



Given : In $\triangle DEF$, $DE^2 + EF^2 = DF^2$

$\triangle XYZ$ is constructed such that :

$XY = DE$, $YZ = EF$ and $\angle Y = 90^\circ$.

Prove that :

$\triangle DEF$ is a right angled triangle.

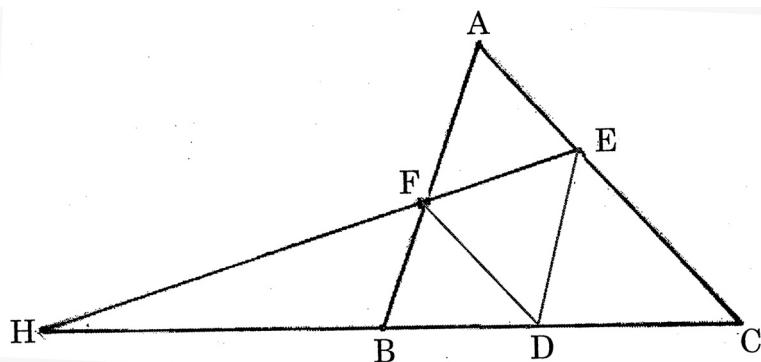


C) Given : D is any point on side BC of $\triangle ABC$. $DE \parallel AB$ and $DF \parallel AC$.

A – F – B and A – E – C. EF and CB meet at H when produced as shown in the fig. Prove that :

[3]

$$HD^2 = HB \times HC$$

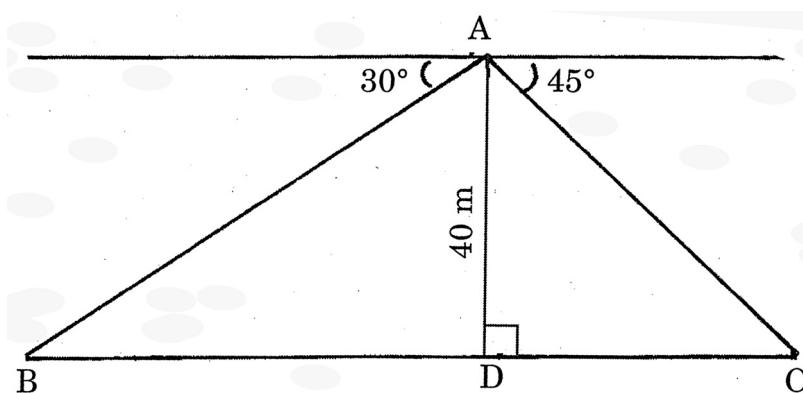


(Write only the proof with reasons)

D) From a point A on a bridge across a river BC, the angle of a depression of the banks on opposite sides of river, B and C are 30° and 45° respectively. If the bridge is at a height of 40 m as shown in the fig., find the width of the river BC.

$$(\sqrt{3} = 1.732)$$

[3]





8. A) Select and write the most appropriate alternative from those given below :

i) The area of the circle that can be inscribed in a square of side 8 cm is

[1]

- a) 8π b) 16π c) 32π d) 64π

ii) If the surface area of a sphere is $196\pi \text{ cm}^2$, then its radius is _____ cm.

[1]

- a) 7 b) 9 c) 11 d) 13

B) Attempt the following :

i) Find the area swept in one minute by a minute hand of a clock of length 12 cm. (Do not substitute for π)

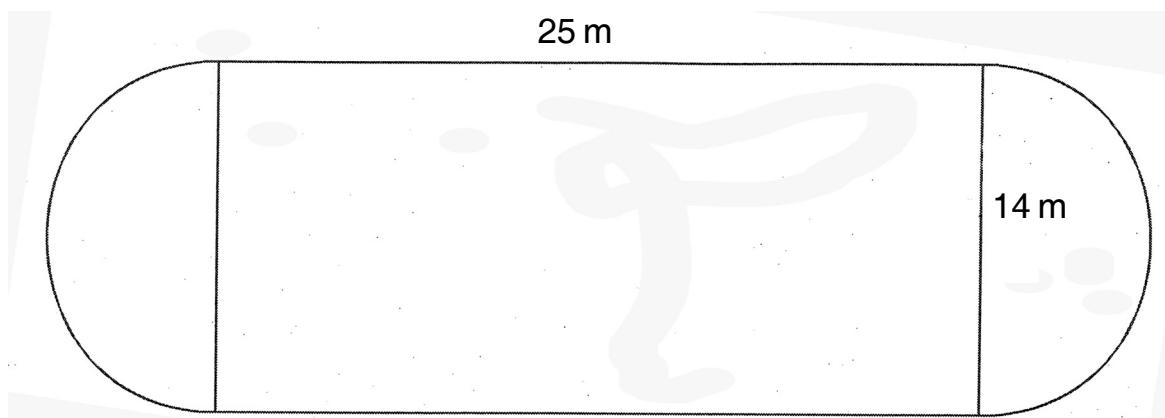
[1]

ii) Find the curved surface area of a right circular cylinder of diameter 7 cm and height 11 cm. (Take $\pi = \frac{22}{7}$).

[1]

C) A flower bed in the form of a rectangle of dimensions $25 \text{ m} \times 14 \text{ m}$ with semicircles on the outer side of the shorter sides of the rectangle as shown in the fig. Calculate the number of rose plants that can be planted if each plant requires $2\text{m} \times 2\text{m}$ area.

[3]



D) A right circular cylinder having radius 6 cm and height 15 cm is full of ice-cream. The ice-cream is to be filled in cones of height 12 cm and radius 3 cm having a hemispherical top. Find the number of such cones that are

required to empty the cylinder. (Take $\pi = \frac{22}{7}$).

[3]